

## 山西特岗答案

### 一、选择题

6、D、2

7、B、" $\exists x_0 \in [2, +\infty), x_0^2 + \tan x_0 + 1 \leq 0$ "

8、A、{1,4}

9、B、第二象限角

10、D、 $-\sqrt{5}$

11、D、函数具有中心对称性，对称中心为 $(\frac{\pi}{2} + k\pi, 0), k \in \mathbb{Z}$

12、B、 $\frac{33}{2}$

13、A、 $\frac{9}{2}\pi$

14、A、 $\frac{5}{4}\pi$

15、D、 $c > b > a$

16、C、 $4\sqrt{2}$

17、A、20200

### 二、填空题

18.  $\frac{1}{4}$

19.  $[\frac{\pi}{3} + 2k\pi, \frac{2\pi}{3} + 2k\pi]$

20.  $4x - y - e = 0$

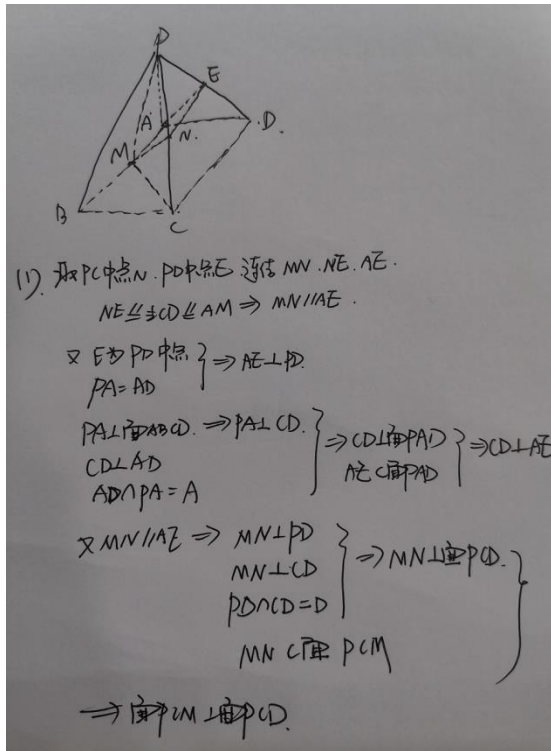
21.  $[\frac{1}{6}, \frac{5}{6}] \cup \{\frac{7}{8}\}$

三、解答题.

22、(1)  $a_n = 2n - 1$

(2)  $T_n = \frac{n}{2n+1}$

23、答案：(1) 见简析 (2)  $\frac{2\sqrt{3}}{3}$



24. 答案：(1)  $P_1 = \frac{1}{28}$  (2)  $E(x) = 1$

(1)  $P_1 = \frac{C_3^1 C_6^1 A_3^3}{A_9^4} = \frac{1}{28}$

解析：

(2)
 

P	0	1	2	3
X	$\frac{8}{27}$	$\frac{4}{9}$	$\frac{1}{9}$	$\frac{1}{27}$

$P(x=0) = C_3^0 \left(\frac{1}{3}\right)^0 \times \left(1 - \frac{1}{3}\right)^3 = \frac{8}{27}$   
 $P(x=1) = C_3^1 \left(\frac{1}{3}\right)^1 \times \left(1 - \frac{1}{3}\right)^2 = \frac{4}{9}$   
 $P(x=2) = C_3^2 \left(\frac{1}{3}\right)^2 \times \left(1 - \frac{1}{3}\right)^1 = \frac{1}{9}$   
 $P(x=3) = C_3^3 \left(\frac{1}{3}\right)^3 \times \left(1 - \frac{1}{3}\right)^0 = \frac{1}{27}$

$\therefore E(x) = 3 \times \frac{1}{3} = 1$

25、答案：(1)  $\frac{x^2}{2} + y^2 = 1$  (2)  $\frac{5}{8}$

26、(1) 见解析 (2) 见解析

(1) 要证:  $\frac{x_1 - x_2}{2n x_1 x_2} < \frac{x_1 + x_2}{2}$   
 即证:  $2n \frac{x_2}{x_1} > \frac{2(x_2 - x_1)}{x_1 + x_2}$   
 即证:  $2n \frac{x_2}{x_1} > \frac{2(\frac{x_2}{x_1} - 1)}{1 + \frac{x_2}{x_1}}$   
 $\frac{2}{2} x = \frac{x_2}{x_1}$   
 $f(x) = 2x - \frac{2(x-1)}{x+1} > 0$   
 $f'(x) = \frac{1}{x} - \frac{2}{(x+1)^2} = \frac{(x+1)^2 - 2x}{x(x+1)^2} > 0$   
 $\therefore f(x)$  在  $x > 1$  时单调递增.  
 $\therefore f(1) = 0$   
 $\therefore f(x) > 0$  在  $x > 1$  时恒成立  
 $\therefore \frac{x_1 - x_2}{2n x_1 - 2n x_2} < \frac{x_1 + x_2}{2}$

(2) 由  $f(x) = 0 \Rightarrow 2x + ae^x = 0 \Rightarrow e^x = -\frac{2x}{a}$   $x_1, x_2$  为方程根  
 今  $x_1 < x_2$   
 $\text{则 } e^{x_1} = -\frac{2x_1 - 1}{a} \quad \text{①}$   
 $e^{x_2} = -\frac{2x_2 - 1}{a} \quad \text{②}$   
 $\frac{\text{②}}{\text{①}} \Rightarrow e^{x_2 - x_1} = \frac{x_2 - 1}{x_1 - 1}$   
 $x_2 - x_1 = \ln \frac{x_2 - 1}{x_1 - 1}$   
 $x_2 - x_1 = \ln(x_2 - 1) - \ln(x_1 - 1)$   
 $\text{证 } (x_2 - 1) - (x_1 - 1) = \ln(x_2 - 1) - \ln(x_1 - 1)$   
 $\frac{(x_2 - 1) - (x_1 - 1)}{\ln(x_2 - 1) - \ln(x_1 - 1)} = 1$   
 又由(1)得  $\frac{x_1 - x_2}{\ln x_1 - \ln x_2} < \frac{x_1 + x_2}{2}$   
 $\therefore \frac{(x_2 - 1) - (x_1 - 1)}{\ln(x_2 - 1) - \ln(x_1 - 1)} < \frac{x_1 + x_2 - 2}{2}$   
 $\therefore \frac{x_1 + x_2 - 2}{2} > 1$   
 $x_1 + x_2 - 2 > 2$   
 $x_1 + x_2 > 4$